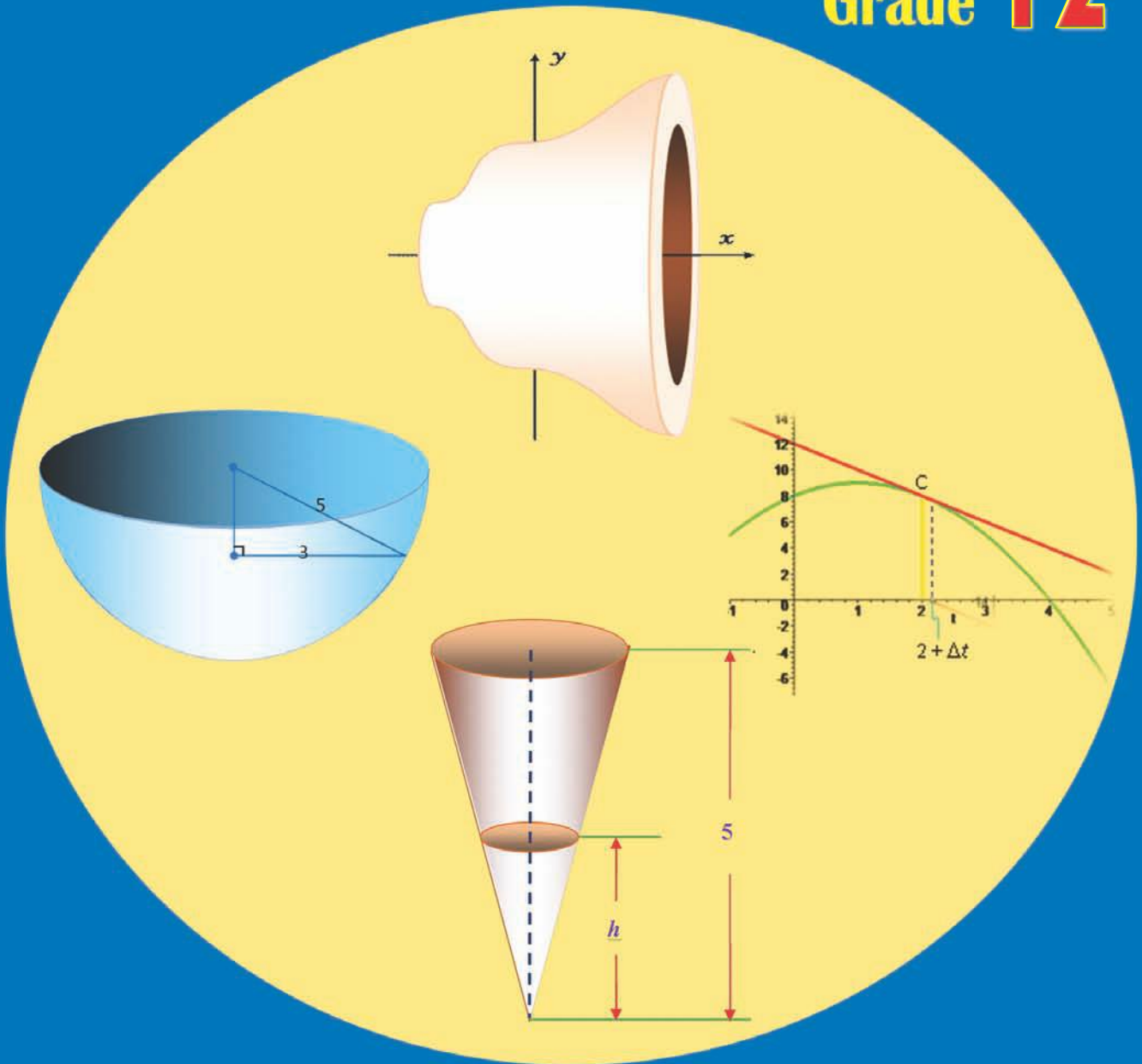




MATHEMATICS

STUDENT TEXTBOOK Grade 12



FEDERAL DEMOCRATIC REPUBLIC OF ETHIOPIA
MINISTRY OF EDUCATION

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MATHEMATICS

STUDENT TEXTBOOK

GRADE 12

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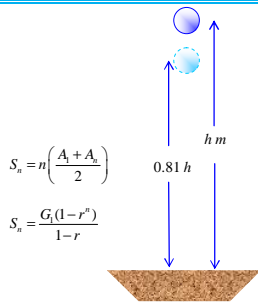
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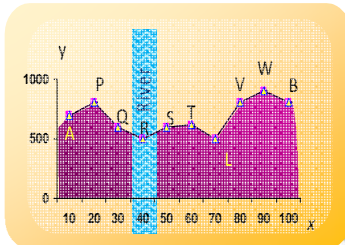
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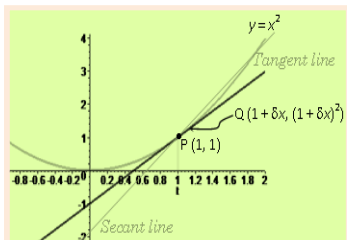
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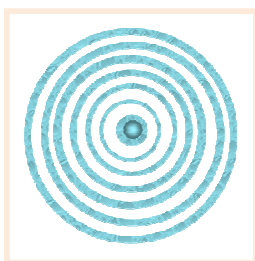


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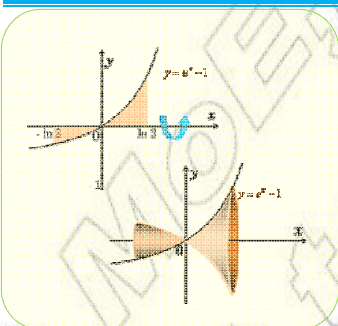
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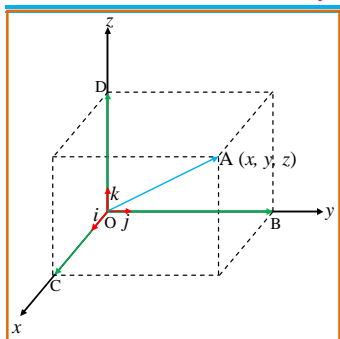
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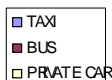
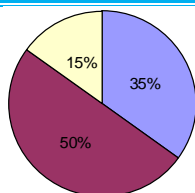
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